## Properties of Solutions

Almost all the chemical processes which occur in nature, whether in animal or vegetable organisms, or in the nonliving surface of the earth, ... take place between substances in solution."

Friedrich Wilhelm Ostwald, 1890
(Nobel Prize for Chemistry in 1909 "in recognition of his work on catalysis and for his investigations into the fundamental principles governing chemical equilibria and rates of reaction".)

Exam II - everything from last exam - Ch 5, 13, 16 (selected sections), 17

### 17.4 Vapor Pressures of Solutions

17.5 Boiling Point Elevation/Freezing Point Depression
17.6 Osmotic Pressure
17.7 Electrolyte Solutions
17.8 Colloids (omit)
midterm grades available tomorrow morning myuic.edu

## Colligative Properties

depend on relative number of dissolved solute particles classification
seen on phase diagram

1. vapor pressure lowering
2. boiling point elevation
3. freezing point depression not on phase diagram
4. osmosis


## Solution Composition

homogeneous mixture of two or more components in a single phase composition
solute - substance being dissolved, usually minor component solvent - dissolving medium, generally major component
expressing composition
mass percent - (mass of solute) / (mass of solvent) $\times 100$
molarity, M - (moles of solute) / (1 L of solution)
mole fraction, $\chi_{\mathrm{A}}-$ for two component solution $\mathrm{A}, \mathrm{B} \chi_{\mathrm{A}}=n_{\mathrm{A}} I\left(n_{\mathrm{A}}+n_{\mathrm{B}}\right)$ molality, $m$ - (moles of solute) / (1 kg of solvent) - independent of temperature, unlike molarity

## Molarity and Molality

EX 2. A 5.50 weight percent sulfuric acid $(M=98.0778)$ solution has a density of $1.0352 \mathrm{~g} \mathrm{~cm}^{-3}$.
a) What is the molarity of the solution?

$$
\begin{aligned}
\mathrm{M}=n / \mathrm{L}= & (5.50 \mathrm{~g} / 100 \mathrm{~g} \text { sol'n })(1 \mathrm{~mol} / 98.0778 \mathrm{~g})(1.0352 \mathrm{~g} \text { sol'n } / \mathrm{mL}) \\
& \times(1000 \mathrm{~mL} / \mathrm{L})=0.581 \mathrm{M}
\end{aligned}
$$

b) What is the molality of the solution?

$$
m=n / \mathrm{kg}=[5.50 \mathrm{~g} /(100-5.50 \mathrm{~g} \text { water })](1 \mathrm{~mol} / 98.0778 \mathrm{~g})(1000 \mathrm{~g} / \mathrm{kg})
$$

## Vapor Pressure and Raoult's Law

The vapor pressure of the solvent above a solution containing a nonvolatile solute is proportional to the mole fraction of the solvent present

Raoult's Law: $\quad P_{\text {solvent }}=\chi_{\text {solvent }} P_{\text {solvent }}^{0}$ (linear function)

EX 3. The vapor pressure of water at $90^{\circ} \mathrm{C}$ is 525.8 mm Hg . If a solution of 651 g of ethylene glycol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}\right)$ is dissolved in 1.50 kg of water, what is the solution vapor pressure at $90^{\circ} \mathrm{C}$ ? $\left(M_{\mathrm{H} 2 \mathrm{O}}=18.02, M_{\mathrm{C} 2 \mathrm{H} 6 \mathrm{O} 2}=62.07 \mathrm{~g} / \mathrm{mol}\right)$

$$
P_{1}=\chi_{1} P_{1}^{0}=(1500 / 18.002) /(1500 / 18.02+651 / 62.07) \times 525.8
$$

## Deviations of Raoult's Law

$$
P_{\text {solvent }}=\chi_{\text {solvent }} P^{0}{ }_{\text {solvent }}
$$

Nonideal solutions show deviations from Raoult's law
negative deviations - strong solute/solvent interactions
positive deviations - weak solute/solvent interactions (weaker than pure liquids)


## Raoult's Law for Determining Molar Mass

1 solvent, 2 solute
EX 4. 20.0 g of urea is dissolved in 125 g of water $\left(M_{\mathrm{H} 2 \mathrm{O}}=18.0148\right)$ at $25^{\circ} \mathrm{C}$. The vapor pressure of the solution was observed to be 22.67 mm Hg . The vapor pressure of pure water at $25^{\circ} \mathrm{C}$ is 23.76 mm Hg . What is the molar mass of urea?

$$
\begin{aligned}
& M=\operatorname{mass} / n \quad P_{1}=\chi_{1} P_{1}^{o}=>\chi_{1}=P_{1} / P_{1}^{\circ}=n_{1} /\left(n_{1}+n_{2}\right) \\
& n_{1} P_{1}^{o}=\left(n_{1}+n_{2}\right) P_{1} \text { or } n_{1} P_{1}^{o}-n_{1} P_{1}=n_{2} P_{1}=> \\
& n_{2}=\text { mass } / M=n_{1}\left(P_{1}^{o}-P_{1}\right) / P_{1} \\
& M=(\operatorname{mass}) P_{1} /\left[n_{1}\left(P_{1}^{\circ}-P_{1}\right)\right]=20.0(22.67) /[(125 / 18.0148)(23.76- \\
& 22.6)]
\end{aligned}
$$

## Deviations from Raoult's Law Ideal Behavior

$$
P_{\text {total }}=P_{\mathrm{A}}+P_{\mathrm{B}}=\chi_{\mathrm{A}} P_{\mathrm{A}}^{\mathrm{o}}+\chi_{\mathrm{B}} P_{\mathrm{B}}^{\mathrm{o}}
$$


(a)

Weak A/B Interactions (compared to pure liquids)

(b)

Strong A/B Interactions

(c)

## Henry's Law (for Solutes)

It is experimentally found that in the limiting case of a solution very dilute in the solute 2 , the partial pressure of 1 in the vapor is directly proportional to the mole fraction of 2 in the liquid.

$$
P=\chi_{\text {gas }} k_{\mathrm{H}}
$$

where $k_{H}$ is the Henry's law constant for the solution.

$$
P_{\text {solvent }}=\chi_{\text {solvent }} P_{\text {solvent }}
$$

Note: this is not Raoult's law behavior where the linear relationship is with the mole faction of the solvent, 1.


## Henry's Law (for Solutes)

1,750 people ${ }^{[3]}$ and 3,500 livestock suffocated

## Table 17.3

The Values of Henry's Law Constants for Several Gases Dissolved in Water at 298 K

| Gas | $k_{\mathrm{H}}(\mathrm{atm})$ |
| :--- | :---: |
| $\mathrm{CH}_{4}$ | $4.13 \times 10^{2}$ |
| $\mathrm{CO}_{2}$ | $1.64 \times 10^{3}$ |
| $\mathrm{O}_{2}$ | $4.34 \times 10^{4}$ |
| CO | $5.71 \times 10^{4}$ |
| $\mathrm{H}_{2}$ | $7.03 \times 10^{4}$ |
| $\mathrm{~N}_{2}$ | $8.57 \times 10^{4}$ |

Lake Nyos, Cameron


## Raoult's Law and a Binary Solution

For an ideal binary solution of $A$ and $B$ the partial pressure of each component above the solution obeys Raoult's law and Dalton's law

$$
P_{\text {total }}=P_{\mathrm{A}}+P_{\mathrm{B}}=\chi_{\mathrm{A}} P_{\mathrm{A}}^{\mathrm{o}}+\chi_{\mathrm{B}} P_{\mathrm{B}}^{\mathrm{o}}
$$

Since both the liquid and gas compositions can be given in terms of mole fractions it is helpful to distinguish between them. The following equations are useful for dealing with binary solutions

$$
P_{\mathrm{A}}=\chi_{\mathrm{A}}^{L} P_{\mathrm{A}}^{\mathrm{o}}\left(\chi^{\text {liquid }}\right) \quad P_{\mathrm{A}}=\chi^{V}{ }_{\mathrm{A}} P_{\text {tot }}\left(\chi^{\text {vapor }}\right) \quad P_{\text {tot }}=P_{\mathrm{A}}+P_{\mathrm{B}} \text { (vapor) } \quad \chi_{\mathrm{A}}+\chi_{\mathrm{B}}=1
$$

## Raoult's Law for Binary Solution (Upstairs/Downstairs)

EX 5. A mixture of hexane ( $P_{1}{ }_{1}=0.198$ ) and heptane ( $P^{\circ}=0.060$ ) obeys Raoult's law. If the mole fraction of heptane is 0.600 , what is the composition of the vapor above the solution?

Strategy:

## DOWNSTAIRS

use Raoult's law to find vapor pressure of each component
UPSTAIRS
sum to get total vapor pressure use Dalton's law to get vapor composition


Aqueous
solution

UPSTAIRS
$P_{\text {tot }}=P_{\mathrm{A}}+P_{\mathrm{B}}$ $P_{\mathrm{A}}=\chi^{\mathrm{V}}{ }_{\mathrm{A}} P_{\text {tot }}\left(\chi^{\text {vapor }}\right)$

DOWNSTAIRS $P_{A}=\chi^{L}{ }_{A} P_{A}{ }_{A}\left(\chi^{\text {liquid }}\right)$

BOTH
$\chi_{A}+\chi_{B}=1$

## Raoult's Law for Binary Solution (Upstairs/Downstairs)

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$$
\begin{aligned}
& P_{1}=\chi^{\mathrm{L}}{ }_{1} P_{0}^{\mathrm{o}}(0.400)(0.198)=0.0792 \\
& P_{2}=\chi_{2}^{\mathrm{L}} P_{2}^{\mathrm{o}}(0.600)(0.060)=0.0360 \\
& P_{\text {tot }}=0.0792+0.0360=0.1152
\end{aligned}
$$


in gas phase

$$
\begin{aligned}
P_{1}=\chi_{1}^{\vee} P_{\text {tot }}=>\chi_{1}^{\vee}=P_{1} / P_{\text {tot }}=0.0792 / 0.1152 & =0.688 \\
\chi_{2}^{\vee}=1.00-0.688 & =0.312
\end{aligned}
$$

## Boiling Point Elevation and Freezing Point Depression

A nonvolatile solute elevates the boiling 1 atm point of a solution

$$
\Delta T=K_{\mathrm{b}} m_{\text {solute }}
$$

and depresses the freezing point

$$
\Delta T=-K_{\mathrm{f}} m_{\text {solute }}
$$

Consider the solvent with a nonvolatile dissolved solute (volatility immaterial for freezing point depression). For freezing point depression assume that the solute does not freeze out of solution. Only the pure solid solvent freezes out when it is cooled to its freezing point.


## Boiling Point Elevation for Molar Mass

EX 6. A solution prepared from 1.25 g of oil of wintergreen (methyl salicylate) in 99.0 g of benzene ( $T_{\mathrm{b}}=80.10^{\circ} \mathrm{C}, K_{\mathrm{b}}=2.3 \mathrm{~K} \mathrm{~kg} \mathrm{~mol}^{-1}$ ) has a boiling point of $80.31^{\circ} \mathrm{C}$. Determine the molar mass of the compound.
$\Delta T=K_{\mathrm{b}} \boldsymbol{m}_{\text {solute }}$
$(80.31-80.10)=\left(2.3 \mathrm{~K} \mathrm{~kg} \mathrm{mo1}^{-1}\right)[(1.25 \mathrm{~g} / \mathrm{M}) / 99.0 \mathrm{~g}] \times 1000 \mathrm{~g} / \mathrm{kg}$

$$
\begin{aligned}
0.21 & =2.3[(1.25 / \mathrm{M}) / 99.0](1000) \\
\Rightarrow> & =150 \mathrm{~g} / \mathrm{mol}
\end{aligned}
$$

## Boiling Point Elevation / Freezing Point Depression

$$
\Delta T_{b}=K_{b} m_{\text {solute }}
$$

$$
\Delta T_{\mathrm{f}}=-K_{\mathrm{f}} m_{\text {solute }}
$$

molality
Table 17.5
Molal Boiling-Point Elevation Constants ( $K_{\mathrm{b}}$ ) and Freezing-Point Depression Constants ( $K_{f}$ ) for Several Solvents

|  | Boiling <br> Point <br> $\left({ }^{\circ} \mathrm{C}\right)$ | $K_{\mathrm{b}}$ <br> $\left({ }^{\circ} \mathrm{C} \mathrm{kg} / \mathrm{mol}\right)$ | Freezing <br> Point <br> $\left({ }^{\circ} \mathrm{C}\right)$ | $K_{\mathrm{f}}$ <br> $\left({ }^{\circ} \mathrm{C} \mathrm{kg} / \mathrm{mol}\right)$ |
| :--- | :---: | :---: | :---: | :---: |
| Solvent | 100.0 | 0.51 | 0. | 1.86 |
| Water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ | 76.5 | 5.03 | -22.99 | 30. |
| Carbon tetrachloride $\left(\mathrm{CCl}_{4}\right)$ | 61.2 | 3.63 | -63.5 | 4.70 |
| Chloroform $\left(\mathrm{CHCl}_{3}\right)$ | 80.1 | 2.53 | 5.5 | 5.12 |
| Benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$ | 46.2 | 2.34 | -111.5 | 3.83 |
| Carbon disulfide $\left(\mathrm{CS}_{2}\right)$ | 34.5 | 2.02 | -116.29 | 1.79 |
| Ethyl ether $\left(\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}\right)$ | 208.0 | 5.95 | 179.8 | 40. |
| Camphor $\left(\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}\right)$ |  |  |  |  |

## Osmotic Pressure

The movement of solvent through a barrier (semipermeable membrane) into a solution containing a solute creates a pressure, P , called the osmotic pressure. This pressure is the extra pressure that must be applied to the solution to maintain equilibrium between the solutions on either side of the barrier.


A tube with a bulb on the end is covered by a semipermeable membrane. The solution inside the tube is surrounded by pure solvent. There is a net transfer of solvent molecules into the solution until the hydrostatic pressure equalizes the solvent flow in both directions and equilibrium is reached.
height proportional to osmotic pressure

$$
\Pi=M R T
$$



## Osmotic Pressure

EX 7. $1.00 \times 10^{-3} \mathrm{~g}$ of a protein is dissolved in 1.00 mL of water. The osmotic pressure of the solution is found to be 1.12 mm Hg at $25^{\circ} \mathrm{C}$. What is the molar mass of the protein?

## Osmotic Pressure

EX 7. $1.00 \times 10^{-3} \mathrm{~g}$ of a protein is dissolved in 1.00 mL of water. The osmotic pressure of the solution is found to be 1.12 mm Hg at $25^{\circ} \mathrm{C}$. What is the molar mass of the protein?

$$
\left.\begin{array}{rlrl}
\Pi=M R T \Rightarrow \Pi V & =n R T \quad n=\text { mass } / M \quad \quad(M \text { molarity }, \\
& =\text { mass } R T / M
\end{array} \quad M \text { molar mass }\right) ~ \$
$$

$M=\operatorname{mass} R T / \Pi V$
$=\left(1.00 \times 10^{-3} \mathrm{~g}\right)(0.08206)(298.15) /(1.12 / 760)\left(1.00 \times 10^{-3} \mathrm{~L}\right)$
$=1.66 \times 10^{4} \mathrm{~g} / \mathrm{mol}$

## Osmotic Pressure



Normal flow of solvent into the solution (osmosis) can be prevented by applying an external pressure to the solution. Minimum pressure required to stop osmosis is equal to the osmotic pressure of the solution.


Reverse osmosis. Pressure greater than the osmotic pressure of the solution applied, which causes a net flow of solvent (blue) from the solution to the pure solvent leaving solute molecules (green) behind.

## Dialysis

Osmosis is a critical property of solvents in biology. It keeps a balance between the interior and exterior of cells and other biological systems. Since the cell wall is semipermeable it behaves as a semipermeable membrane. Small molecules and water can pass through the cell wall but large molecules (such as DNA and proteins) generally cannot. Therefore there is a higher concentration of particles inside the cell (colligative effect).


A typical dialysis membrane has a pore size of about 24 angstroms which excludes large macromolecules but allows water and small molecules to pass through.

## Biological Solutions

Consider a transfusion or even administration of a saline solution. One needs to input a solution of similar osmotic properties (isotonic) to avoid having too dilute a solvent (hypotonic) which will go into the cell and raise pressure and cause rupture or too concentrated a solution (hypertonic) which extracts the solvent and collapses the cell.


